

Math 410 – Number Theory

Course Description from Bulletin: Divisibility, congruences, distribution of prime numbers, functions of number theory, diophantine equations, applications to encryption methods. (3-0-3)

Enrollment: Elective for AM and other majors.

Textbook(s): Burton, *Elementary Number Theory*, 6th Edition, McGraw-Hill.

Other required material: Occasional handouts

Prerequisites: MATH 230 or consent of the instructor

Objectives:

1. Students will achieve command of the fundamental definitions and concepts of number theory.
2. Students will understand and apply the core definitions and theorems, generating examples as needed.
3. Students will become proficient in writing proofs in elementary number theory.

7. Quadratic Reciprocity 6
 Quadratic Congruences, Quadratic Residues and Nonresidues, Euler's
 Criterion, the Legendre Symbol & its properties, Gauss' Lemma, Germain
 Primes (& primes of the form $4k+1$ and $8k-1$), the Quadratic Reciprocity Law,
 $(2/p)$ and $(3/p)$, Quadratic Congruences with Composite Moduli
8. Introduction to Cryptography 3
 Basics, RSA public key cryptography, the ElGamal Cryptosystem
9. Options
- Recent developments in Primality Testing and Factorization (3)
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