

Math 435 – Linear Optimization

Course Description from Bulletin: Introduction to both theoretical and algorithmic aspects of linear optimization: geometry of linear programs, simplex method, anticycling, duality theory and dual simplex method, sensitivity analysis, large scale optimization via Dantzig-Wolfe decomposition and Benders decomposition, interior point methods,

Introduction to both theoretical and algorithmic aspects of linear optimization: geometry of linear programs, simplex method, anticycling, duality theory and dual simplex method, sensitivity analysis, large scale optimization via Dantzig-Wolfe decomposition and Benders decomposition, interior point methods,

Existence and optimality of extreme points	
3. Simplex Method	9
Optimality conditions	
Simplex method	
Revised simplex method and full tableau implementation	
Anticycling: Bland's rule	
Initial basic feasible solution	
Computational efficiency of the simplex method	
4. Duality Theory and Sensitivity analysis	7
Dual linear program	
Duality Theorems and Complementary Slackness	
Dual Simplex method	
Farkas' Lemma and its application to duality theorem	
Sensitivity analysis and Parametric programming	
5. Large Scale Optimization	5
Delayed column generation and Dantzig-Wolfe decomposition	
Cutting plane methods and Benders decomposition	
6. Optional Topics (selected based on class composition and background)	11
Interior Point Methods	
The von Neumann algorithm	
The affine scaling algorithm	
The primal path following algorithm	
Network Flow Problems	
The minimum cost flow problem and the Network simplex algorithm	
The maximum flow problem and the Ford-Fulkerson algorithm	
The assignment problem and the Auction algorithm	
Integer Programming	
Gomory Cuts and Cutting plane algorithms	
Branch and bound	
Dynamic programming	
IP duality and Lagrangian Relaxation	
7. Exams and Overflow	3

Assessment:	Homework	25-50%
	Quizzes/Tests	30-50%
	Final Exam	25-40%

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